# CURVELET BASED WATERMARKING OF MULTISPECTRAL IMAGES AND ITS EFFECT ON CLASSIFICATION ACCURACY


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***Abstract*—In this paper, a robust invisible watermarking algorithm for satellite imagery using Curvelet Transform is proposed. Haralick Co-occurrence texture features [1] are used to identify the area for watermarking in the host image. Host image is tiled into smaller non-overlapping blocks. Based on the Haralick texture feature chosen, blocks with high value of chosen texture feature were selected for embedding. Thus, multiple watermarks are embedded in any given image. There are some unstable Curvelet coefficients so a little change of the image will result in a big change of these coefficients. These unstable factors can influence the extracting of watermark. Hence selection of position of embedding in the transformed domain plays a very important role in robustness of the embedding process. This algorithm encourages use of edges and curves for embedding watermarks. The experimental results show that watermark using proposed algorithm is robust against common attacks like Brightness, Contrast, Saturation, Tint adjustments, Low pass Filtering, JPEG Compression attack, Gaussian Noise attack and Laplacian Filtering, Symmetrical and Asymmetrical Image Cropping, Geometric Attacks like scaling and Rotation. Use of SURF features [2] too ensures robustness to geometric attacks. The effect of watermarking on the classification accuracy is also studied.**



***Keywords***- *Curvelet, Wavelet, co-occurrence texture, watermark, Satellite, texture, Robust, Classification*


## I. INTRODUCTION

Geospatial data or geographic data identifies the geographic location of features and boundaries on Earth, such as natural or constructed features, oceans, and more. Geographic Information have long been used in diverse applications for commercial, scientific and defense use. Satellite imagery forms one of the most frequently used geographic data and with the level of detail that this imagery can reveal in today's technology, the data has significant strategic and commercial value. Techniques like inpainting can alter the content and illegal access can lead to claims of ownership. Therefore, there is a compelling need for ensuring of authenticity and protection of ownership.

For providing the security of digital data various techniques are used like encryption, decryption, cryptography, and digital watermarking. Digital watermarking is a technique of embedding selected user information into the digital content like image, video, speech, music etc. The watermarking algorithm should be able to detect intentional tampering of the original data and retain its integrity within the content even after various manipulation attacks like compression, enhancement, cropping, filtering etc.

Most natural images/signals exhibit line-like edges, and discontinuities across curves called curve singularities. Candes and Donoho [4] [5] proposed a multiresolution geometric analysis (MGA), named Curvelet transform that not only considers a multiscale time (or space)-frequency local partition but also makes use of the direction of features.

The Curvelet transform directly takes edges as the basic representation element; it provides optimally sparse representations of objects along edges. Candes and Donoho suggested two strategies, namely Unequally-Spaced Fast Fourier Transform (USFFT) and Frequency wrapping. The Wrapping based Curvelet transform technique is conceptually simpler, faster and less redundant than the previous techniques.

A preliminary literature review of past studies shows that watermarking techniques in frequency domain are primarily focused on transforms like Discrete Cosine Transform (DCT), Discrete Wavelet Transform (DWT). Lot of work has been done in field of watermarking in Wavelet Domain. Wavelet based watermarking techniques are robust, popular and efficient. However little work has been made on Invisible watermarking using Discrete Curvelet Transform. In this paper a robust invisible watermarking technique is proposed using the wrapping FDCT method. Primary Objective of watermarking technique proposed in this paper is copyright protection and image authentication.

## II. CURVELET TRANSFORM

Discrete Fourier Transform (DFT) is the most common and powerful procedure to analyze, manipulate and synthesize digital signals. The big disadvantage of a Fourier expansion however is that it provides frequency resolution and no time resolution.

The wavelet transform or wavelet analysis overcomes this shortcoming of the Fourier Transform by giving a time-frequency joint representation. The idea behind these time-frequency joint representations is to cut the signal of interest into several parts and then separately analyzing each part. This gives more information about the when and where of different frequency components.

Natural images usually have line-like edges, i.e., discontinuities across curves, which are called line or curve singularities. However, wavelets cannot represent line singularities. To represent that Curvelet Transform is used.

The Curvelet transform is a multiscale transform like the wavelet transform, with frame elements indexed by scale and location parameters. It preserves the same time frequency localization property as for wavelets and at the same time Curvelet become directional. It acts like a bandpass filter. In addition, anisotropic scaling principle, which is quite different from the isotropic scaling of wavelets, helps in sparse representation. The elements obey a special parabolic scaling law, defined by width ≈ length$^2$. So instead of square representation it is now rectangular representation (**Fig. 1**). By changing the scale location and orientation the multiscalar coefficients can be obtained as shown in **Fig 2** to 4.

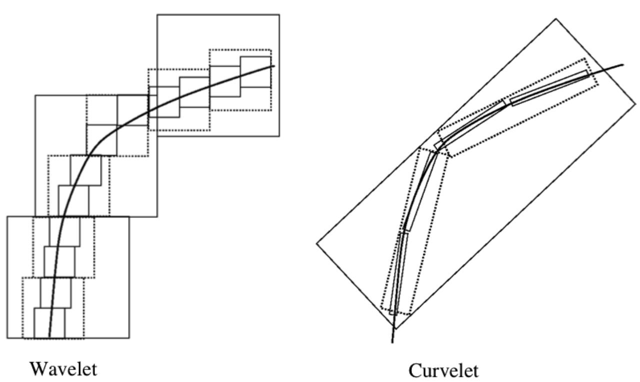



**Fig.1. Parabolic scaling, non-linear approximation [6]**

In Second generation transform Curvelet DCTG2, first 2D Fast Fourier Transform (FFT) of the image is taken. The 2D Fourier frequency plane is then divided into wedges. The partitioning of the Fourier plane into dyadic squares and angular divisions results in parabolic shaped wedges. Each square represents a scale and acts like a bandpass filter and the angular divisions partition the band passed image into different angles or orientations.

**Fig. 2. Curvelet with fixed scale, fixed orientation but variable location [6]**

**Fig. 3. Curvelet with fixed scale, fixed location but variable orientation [6]**

**Fig. 4. Curvelet with fixed orientation, fixed location but variable scale [6]**

Curvelab 2.1.3 software package implements the FDCT_WRAPPING algorithm. The DCTG2 implementation can assign either wavelets or curvelets at the finest scale. Scale (resolution) and angles (no of orientation) can be defined to get varying level of resolution. For the algorithm proposed in this paper, 4 scale - 8 angle wrapping Curvelet transform with curvelets at the finest level is used. The output of a 4 scale - 8 angle Wrapping Curvelet transform results in

**Curvelet Transform output = {1x1} {1x8} {1x16} {1x16}**

{1x1} – Represents the low frequency components
{1x8} - Scale 2. Each of the 8 columns represents data for that angle (wedge)
{1X16} - Scale 3. Each of the 16 columns represents data for that angle (wedge)
{1x16}- Scale 4. Each of the 16 columns represents data for that angle (wedge)

## III. EMBEDDING ALGORITHM

This algorithm incorporates semi-blind robust watermark extraction wherein the original image is not available for extraction; hence a key containing detail about embedding is attached to the watermarked image. Watermark is embedded in the third band of the image.

1. Resize the Host Image to MXN such that M and N are power of 2.
2. Choose a watermark image (A x B) and convert it into binary. Serialize the watermark $W_s$. Ws = {Wk = 1, 2, 3, …, A × B; Wk {−1,1}}
3. Split the Host image into smaller non-overlapping blocks (e.g image size 2048 x 2048 block size is 512 x 512; image size 512 x 512 block size is 64 x 64)
4. Extract co-occurrence texture features for each block. Mark blocks that have high texture feature (as specified by user) for embedding. Deselect 1 row and 1 column of blocks from all the four edges to ensure that no watermarks are lost when borders are cropped.
5. For each marked block do the following
    a. Apply Wrapping Curvelet Transform (fdct_wrapping) with finest level as wavelet, 4 scales and 8 angles. C denotes this Curvelet Transform.
    b. Implement LOCEDGES logic that selects locations and orientation for embedding watermarks in Scale 3 Curvelet coefficients (section III A). arr_max contains orientation and location for embedding $W_k$ = 1 and arr_min contains orientation and location for $W_k$= -1.
    c. For each location in level 3, $S_{3O}$ (i, j), O indicates orientation; there are 4 dependent locations in Scale 4, $S_{4O.}$ (2i, 2j; 2i, 2j-1; 2i-1, 2j; 2i-1, 2j-1). These are called child nodes. Find Max (max_node) and Min (min_node) of these 4 child nodes.
    d. **If** $W_k$ = 1
       select location (i, j) and orientation (O) from arr_max
       C {1,3} {1, O} (i, j) = max_node + alpha
       **else**
       select location (i,j) and orientation (O) from arr_max
       C {1,3} {1, O} (i,j)= min_node - alpha
       **End if**
       The chosen value of alpha = 160, which can be adjusted to change the strength of invisibility.
    e. Apply Inverse wrapping Curvelet transform to get watermarked image.
6. Concatenate all the split blocks (modified and unmodified) to form Host image with multiple embedded watermarks. Resize this image (M x N) to size of original image.
7. Generate a key by using RSA encryption to encrypt following data
    a. SURF features of the watermarked image. This includes features and valid points for each descriptor. This is useful for visualizing the descriptor orientation.
    b. Watermarked location, orientation and original coefficient value of each watermarked block.
    c. Blocks that are watermarked.
    d. Original size of the Host Image and watermark image.

*A. Locedges*

Logic for selecting orientation and locations for embedding watermarks This algorithm chooses edges (high value coefficients) for embedding 1's in watermark and low value coefficients for embedding -1's in watermark.

1. Scan the entire Curvelet coefficients across all orientations in Level 3 and create an array arr_level_max that holds value of maximum coefficient in each orientation.
2. Select the orientation from arr_level_max with maximum coefficient value max_value.
3. Set threshold $T_{max}$=0.5*max_value. Create an array arr_max that holds orientation and location of all coefficient values greater than $T_{max.}$
4. If no. of locations found is less than total no of 1s in watermark repeat step 3 with next highest value from arr_level_max
5. For identifying locations to embed -1s set $T_{min}$=0 and choose all locations in a given orientation which are less than $T_{min.}$

## IV. Extraction Algorithm

1. Check for Geometric Attack (section IV A).
2. Split the Embedded Host Image into smaller non-overlapping blocks with block size same as that in the embedding algorithm.
3. Extract the watermarked blocks from the key.
4. Apply Wrapping Curvelet Transform (fdct_wrapping) with finest level as wavelet, 4 scales and 8 angles. $C_{extract}$ denotes this Curvelet Transform.
5. For every watermarked block
    a. Extract the Watermarked location (i, j), orientation (O) and original value (org_val) of each watermarked block.
    b. If $C_{extract}$. {1,3} {1,0} (i,j) > org_val, $W_k$=1
       Else $W_k$=-1.
6. Reshape the serial Watermark into 2D depending of size extracted from key.

*A. Algorithm to Check Geometric Attack*

1. Extract the SURF Features of the original embedded image from the key.
2. Find the SURF Features of the altered embedded image.
3. Find the matching points between the original and altered images using estimate Geometric Transform.
4. Restore the image using imwarp. (This takes care of the size and rotation attacks)

Another technique for detecting Geometric attacks is using Radon Transform where the maximum value in the Radon transform can be used to detect scale change and the rotation can be detected by location of the maximum value. However, this cannot detect any asymmetrical cropping of the image and hence algorithm using SURF features provides a robust solution to detecting geometric attacks and asymmetrical cropping. SIFT features could also be used, however this was not explored.

## V. Results and Discussion

A host image is satellite image of Mumbai SAT5 (1153 x 1153) (SIP LAB, CSRE, IIT Bombay) and watermark image was of size 7x22. Robustness of algorithm for a variety of watermarking attacks was tested.

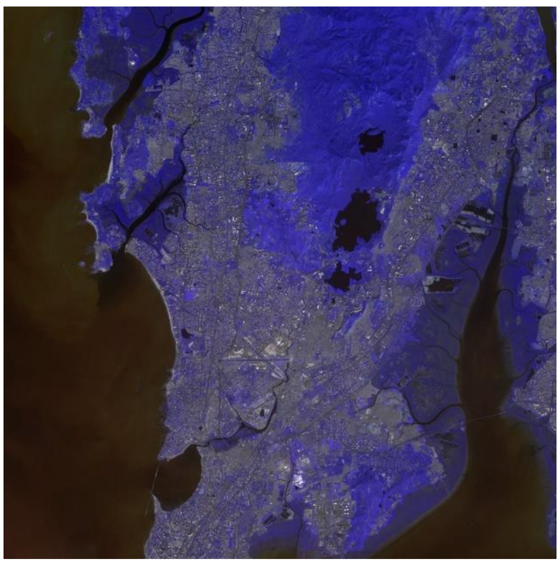


**Fig. 5. Host Image SAT5 (1856 x1404)**


**Fig.6. Watermarking Image 7x22**

Response to 6 attacks viz. Compression, Gaussian Noise, Geometric attack, Contrast adjustment, smoothing (neighborhood filtering), is tabulated below (Table I to VIII):

**Table I Notation Used in Results**

| ***Notations*** | ***Details*** |
|---|---|
| #W embedded | No of watermarks embedded |
| #W retrieved | No of watermarks extracted correctly |
| CPSNR | Cumulative PSNR (For all watermarks) |
| CMSE | Cumulative MSE (For all watermarks) |

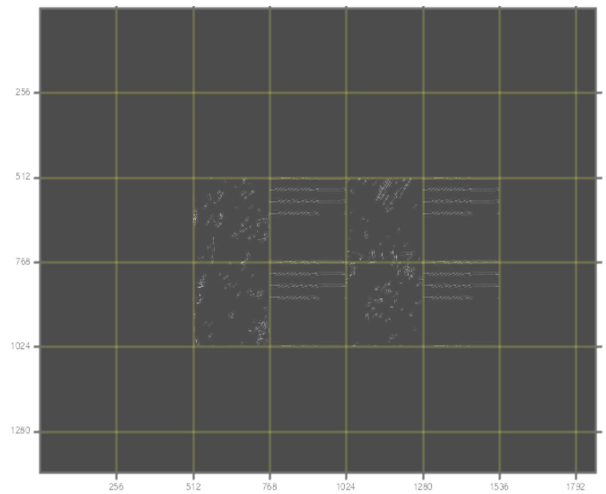



**Fig.7. Difference between the Host image and Curvelet Watermarked image. Note that there are 8 watermarked blocks and the dashes indicate watermarking**

Table VIII shows the samples of retrieved watermarks in various attack.

Fig. 8 and Fig. 9 shows the watermarked images with 29 and 245 watermarks respectively. Visual inspection of the watermarked image shows that there is not much change in perceptual quality of the image after watermarking. Fig. 10 shows Classified image without watermark. Fig. 11 and Fig. 12 shows classified image with 29 and 245 watermarks. Table IX and X is classification accuracy for training area and test area respectively

**Table II Results of Gaussian noise attack**

| ***% Noise in dB*** | ***Curvelet Watermarking*** | | | |
|---|---|---|---|---|
| | ***#W embedded*** | ***#W extracted*** | ***CPSNR*** | ***CMSE*** |
| 10 | 8 | 0 | 65.36 | 4.7 |
| 15 | 8 | 8 | Infinity | 0 |
| 20 | 8 | 8 | Infinity | 0 |
| 25 | 8 | 8 | Infinity | 0 |
| 30 | 8 | 8 | Infinity | 0 |

**Table III Results of Gaussian Attack**

| ***Scaling (S), Rotation (R) Factor*** | | ***Curvelet Watermarking*** | | | |
|---|---|---|---|---|---|
| | | ***#W embedded*** | ***#W extracted*** | ***CPSNR*** | ***CMSE*** |
| ***S*** | ***R*** | | | | |
| 1 | 2 | 8 | 7 | 70.06 | 1.20 |
| 1 | 4 | 8 | 6 | 67.62 | 3.89 |
| 1 | 6 | 8 | 4 | 63.11 | 4.20 |
| 1 | 10 | 8 | 4 | 64.17 | 4.80 |
| 1.2 | 2 | 8 | 6 | 60.45 | 1.56 |
| 1.2 | 4 | 8 | 6 | 58.46 | 4.10 |
| 1.2 | 6 | 8 | 4 | 56.12 | 4.60 |
| 0.21 | 10 | 8 | 4 | 55.43 | 5.10 |

TABLE IV RESULTS OF CONTRAST ENHANCEMENT ATTACK

| ***Technique*** | ***Curvelet Watermarking*** | | | |
|---|---|---|---|---|
| | ***#W embedded*** | ***#W extracted*** | ***CPSNR*** | ***CMSE*** |
| Histogram equalization | 8 | 5 | 70.06 | 1.6 |
| Adjusting Image Intensity to increase contrast | 8 | 8 | Infinity | 0 |
| Contrast-limited adaptive histogram equalization | 8 | 6 | 66.96 | 0.81 |

TABLE V RESULTS OF LOW PASS FILTERING ATTACK

| ***Filter*** | ***Curvelet Watermarking*** | | | |
|---|---|---|---|---|
| | ***#W embedded*** | ***#W extracted*** | ***CPSNR*** | ***CMSE*** |
| Averaging | 8 | 0 | 57.14 | 101 |
| Gaussian LPF (f=10) | 8 | 0 | Infinity | 0 |
| Gaussian LPF (f=100) | 8 | 0 | 57.18 | 112 |
| Gaussian LPF (f=1k) | 8 | 0 | 57.19 | 115 |
| Gaussian LPF (f=10k) | 8 | 0 | 57.19 | 116 |

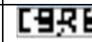
TABLE VI RESULTS OF CROPPING ATTACK

| ***Cropping*** | ***Curvelet Watermarking*** | | | |
|---|---|---|---|---|
| | ***#W embedded*** | ***#W extracted*** | ***CPSNR*** | ***CMSE*** |
| 10% Left | 8 | 8 | Infinity | 0 |
| 10% Right | 8 | 8 | Infinity | 0 |
| 10% Top | 8 | 8 | Infinity | 0 |
| 10% Bottom | 8 | 8 | Infinity | 0 |

TABLE VII HYBRID CURVELET WATERMARKING - LPF ATTACK

| ***Filter*** | ***#W embedded*** | ***#W extracted*** | ***CPSNR*** | ***CMSE*** |
|---|---|---|---|---|
| Averaging | 1 | 0 | 61.55 | 9.09 |
| Gaussian LPF (f=10) | 1 | 0 | 62.22 | 7.79 |
| Gaussian LPF (f=100) | 1 | 0 | 70.06 | 2.28 |
| Gaussian LPF (f=1k) | 1 | 0 | 60.90 | 10.3 |
| Gaussian LPF (f=10k) | 1 | 0 | 62.22 | 7.79 |

TABLE VIII SAMPLES OF RETRIEVED WATERMARKS IN VARIOUS ATTACKS

| ***Attack*** | ***Curvelet Watermarking*** | | | |
|---|---|---|---|---|
| | ***#W embedded*** | ***#W extracted*** | ***Max MSE*** | ***Watermark with Max Error*** |
| 20% Compression | 8 | 0 | 7.79 |  |
| 10 dB Gaussian Noise | 8 | 0 | 3.90 |  |
| Average filter* | 1 | 0 | 9.09 |  |
| Contrast Adjustment Histogram Equalization | 8 | 5 | 1.60 |  |
| Scaling and Rotation (S=1 & R=2) | 8 | 7 | 1.20 |  |

From the above observation, it is evident that the Curvelet watermarking algorithm fails the low pass filtering and averaging attacks. A hybrid-watermarking algorithm in which 80% of the watermarks are embedded in edges 20% watermarks locations are chosen where there is not much variation to overcome impact of LPF attack. Embedding in high frequency coefficients offers better imperceptibility, while low frequency coefficients provides high robustness against Filtering attacks.

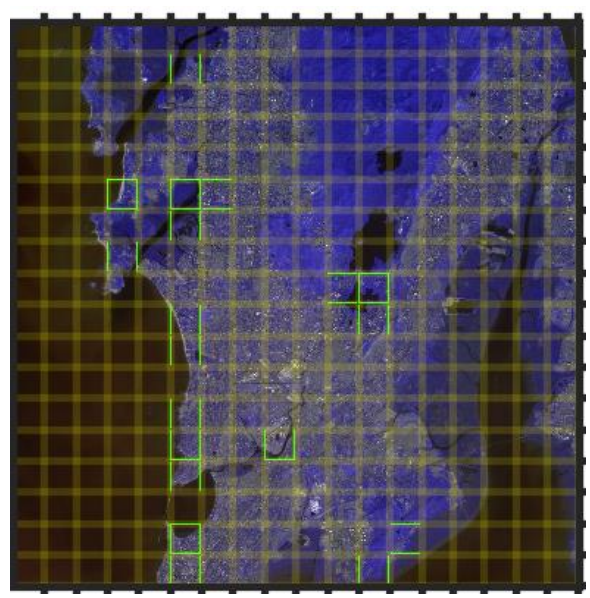


**Fig. 8. Watermarked Image – 29 watermarks**

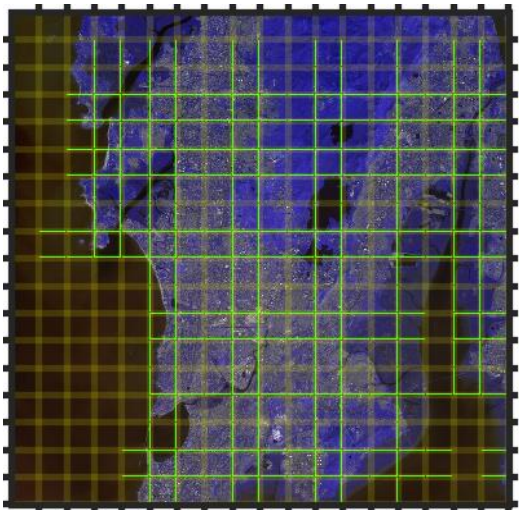


**Fig.9. Watermarked Image – 245 watermarks**

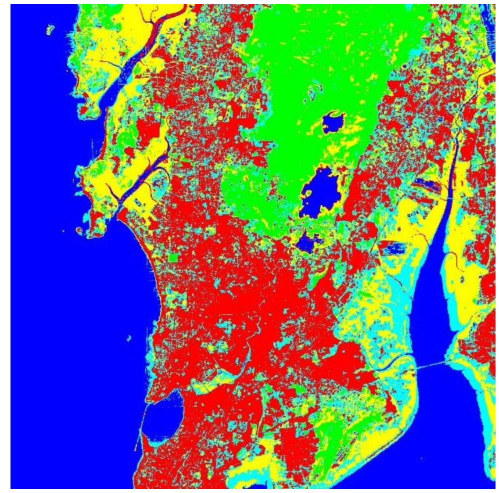


**Fig. 11. Classified Watermarked (29) Image using MLC**

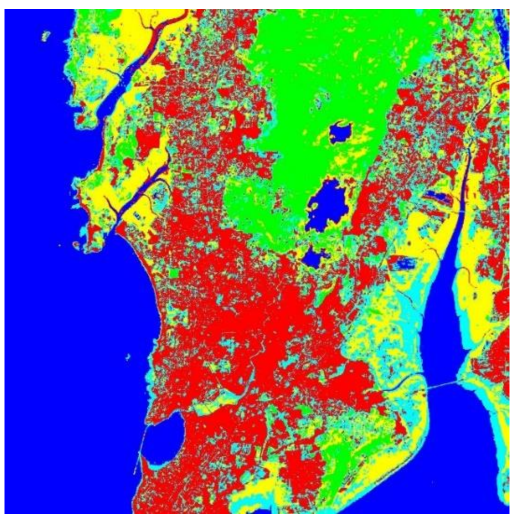


**Fig. 10. Classified Original Image using MLC**

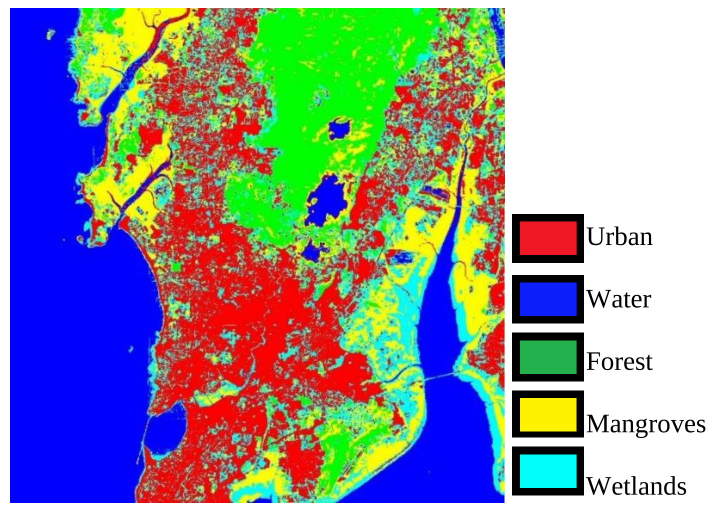



**Fig. 12. Classified Watermarked (245) Image using MLC**

**TABLE IX CLASSIFICATION ACCURACY FOR ORIGINAL AND WATERMARKED IMAGE (IN PERCENTAGE FOR TRAINING AREAS)**

| Class | Without Watermark | Number of Watermarks embedded | | | | |
|---|---|---|---|---|---|---|
| | | 29 | 65 | 202 | 214 | 245 |
| Urban | 99.90 | 99.90 | 99.90 | 99.90 | 99.90 | 99.90 |
| Water | 100.00 | 100.00 | 100.00 | 100.00 | 99.86 | 100.00 |
| Forest | 98.55 | 98.55 | 98.55 | 98.55 | 98.46 | 97.54 |
| Wetland | 98.34 | 98.06 | 97.93 | 98.20 | 98.20 | 98.06 |
| Mangroves | 96.19 | 96.08 | 96.08 | 95.42 | 95.64 | 95.32 |
| **Accuracy** | **99.26** | **99.24** | **99.23** | **99.20** | **99.13** | **98.93** |

**TABLE X CLASSIFICATION ACCURACY OF TEST AREAS (IN PERCENTAGE)**

| Class | Without Watermark | Number of Watermarks embedded | | | | |
|---|---|---|---|---|---|---|
| | | **29** | **65** | **202** | **214** | **245** |
| Urban | 99.82 | 99.82 | 99.87 | 99.87 | 99.87 | 99.87 |
| Water | 100.00 | 100.00 | 100.00 | 99.86 | 99.80 | 99.84 |
| Forest | 97.74 | 97.57 | 97.44 | 95.99 | 96.76 | 95.65 |
| Wetland | 97.69 | 97.69 | 97.20 | 97.32 | 97.20 | 97.56 |
| Mangroves | 96.62 | 97.01 | 97.01 | 96.65 | 96.83 | 96.74 |
| **Accuracy** | **98.98** | **98.95** | **98.90** | **98.65** | **98.50** | **98.45** |

To check the effect of Watermarking on classification accuracy, Maximum Likelihood Classifier (MLC) is used to classify the watermarked and original (without watermark) image. The classified images are shown fig. 10, 11 and 12. The classification accuracy for the original image is 99.26% for training areas and 98.98% for test areas. From table IX and X, it is observed that classification accuracy hardly decreases by inserting 245 watermarks to 98.93% for training areas and 98.45% for test areas.

## VI. CONCLUSION

This new approach for embedding Invisible Watermarking using Curvelet transform shows improved performance over wavelet transform when embedding logic is same. Robustness against variety of attacks is due to use of texture features to select blocks combined with selection of appropriate locations for embedding. Use of SURF features serves in synchronizing embedding location, which helps in detecting and recovering from geometric attacks resulting in negligible MSE. The proposed technique can also be used to watermarked multiband images.

It has been observed that the algorithm is not capable of handling Low pass filtering and average filtering attack. This is as expected because edges in the images are used for embedding watermark. To overcome this drawback a hybrid embedding logic is incorporated where 20% watermarks are embedded in locations that do not have sharp edges.80% watermarks are embedded in edges, this ensures robustness against filtering attacks.

The proposed watermark algorithm using Curvelet does not affect the classification accuracy of the multispectral imagery even when the number of watermarks inserted is substantial. The impact is minimum for waterbodies which are homogenous areas as watermark is inserted in edges. The classification accuracy is 98.95% for 29 watermarks and shows a marginal decrease 98.45% when the watermarks are increased to 245. Instead of MLC non-parametric classifiers like SVM, ANN etc. can be applied to check the results

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